COMMON SUBEXPRESSION INDUCTION †

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SIMD (Single Instruction stream, Multiple Data stream) computers can only execute the exact same instruction across all processing elements. This paper presents a new compiler optimization that transforms multiple distinct code threads so that they have as many instructions in common as possible, hence, SIMD execution time is minimized. For example, SIMD "parallel if" statements typically take the then clause time plus the else clause time to execute, but this new transformation usually can induce identical code sequences for most of the code in the then and else clauses, often yielding a 40% improvement in execution speed. The same principle also could be used to transform code which operates on multiple short vectors into operations on long vectors containing the catenation of the shorter vectors; for example, operations on two 8,192-element arrays might be combined into a single operation apparently acting on a 16,384-element array.

1. Introduction

Traditional compiler analysis and code transformation are based on tracking what happens to **values**, as noted in [4]. For example, in common subexpression elimination (CSE) the compiler recognizes when the **same value** would be computed more than once and rewrites the code to make multiple references to a single computation of that value.

Dependence analysis [2] and alias analysis [7] are different from the above in that they are not so much concerned with values as with **storage locations**. The compiler tries to recognize when references might access the **same storage location**, and can parallelize references in which different storage locations are accessed. Register, cache, and page allocation/management are also based on tracking storage locations.

The interesting point is that there is yet another type of program entity which can be analyzed: the **code** itself. A few compiler transformations, such as code straightening [4], operate directly on the **code** structure, but relatively little attention has been given to this type of analysis and transformation.

Common subexpression induction (CSI)^(a), the topic of this paper, is the **code**-based equivalent of the value-based CSE optimization; CSI recognizes when the **same code** can be used for multiple execution threads. Whereas CSE is clearly

beneficial when the execution time is directly proportional to the number of instructions executed, CSI is most beneficial when the execution time is proportional to the sum of the execution times for all control-flow paths — as in single instruction stream multiple data stream (SIMD) parallel computers.

The following section describes the machine properties that can make the CSI optimization useful. In section 3, each step of the CSI algorithm, and our prototype CSI tool, is explained. A simple example is used to illustrate the analysis and to expose an issue for further research involving the concept of register liveness for parallel machines. Section 4 presents a second, larger and less symmetrical, example. This second example is used to drive a discussion on how the algorithm from section 3 can be made still more efficient for large CSI problems. In section 5, we briefly present an example of how CSI can be used to increase apparent vector length, although we do not present an algorithm for this transformation. In closing, section 6 summarizes the contributions of this paper and directions for further study.

2. Machine Characteristics for CSI

The basic premise of CSI is that some machines have structures that permit a single instruction to compute several different values, hence, for those machines it is useful to be able to induce code structures that can maximize the number of useful values computed by each instruction. In some architectures, an improvement in parallelism results; in others, the primary effect is an improvement in cache performance. Machine architectures that can benefit from CSI include:

- **SIMD**: In a SIMD machine with *N* PEs (Processing Elements), up to *N* values can be computed by a single instruction. However, this performance can only be achieved if all *N* PEs (processing elements) will be executing the same operation PEs that need to execute different operations cannot do useful work in that cycle. Because CSI increases the fraction of PEs that simultaneously execute the same instruction (the useful parallelism width), large speedups can be obtained. Examples of this type of machine include the TMC CM-2 [16] and the MasPar MP-1 [3].
- Vector: Although typically not as parallel, vector machines profit from CSI in essentially the same way that SIMD machines do. A good example of such a machine is the Cray Y-MP C90 [5].
- MIMD with shared I-Cache: CSI, as described in this paper, is directly usable to improve performance of sharedmemory MIMD (Multiple Instruction stream, Multiple Data stream) systems that have instruction caches with a mechanism for sharing. For example, such a sharing mechanism was proposed for the FMP [9] and is generalized in [12].

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⁽a) This name was coined in [7], without a practical algorithm. It refers to the concept that, since some machines can have common subexpressions share the same code, it can be useful to induce such code sequences even if some additional instructions (e.g., register moves) must be inserted.

The logic is simply that if a MIMD is programmed using the SPMD model (Single Program, Multiple Data), separate MIMD processes execute independently, but often are executing the same region of code at about the same time. Hence, sharing an instruction cache can allow trailing processors to reuse the instructions fetched by the leading processors. Clearly, by reducing the number of different control flow threads in the SPMD program, CSI can maximize the regions of code over which this sharing can occur.

- VLIW and Superscalar: Although VLIW (Very Long Instruction Word) [8] and Superscalar machines can execute multiple operations within a single instruction, they also can benefit from a variation on the CSI optimization. The reason is simply that most *N*-PE VLIW machines cannot pack *N* arbitrary operations into a single instruction —there are usually constraints on which operations can be packed together. For example, it is common to see a limit placed on how many load/store operations can be placed in each instruction. This optimization differs from CSI as described in this paper primarily in that the classifi cation algorithm (see section 3.2.4) is somewhat more complex.
- Sequential Nulling versus Jumps: Some processors have instructions that allow the operation to be nulled depending on a condition code. For example, this is the mechanism used to implement "Squashing Branches" [11]. In such a serial machine, CSI can improve performance because it can replace branching overhead (both the branch instruction and the cache behavior it often introduces) with just a few instructions being marked as nullable.

In this paper, we will focus on the application of CSI to massively parallel SIMD machines, in particular, to the MasPar MP-1. This is partly because the expected benefit to SIMD machines is very large, but also because the algorithm and examples are more easily understood. In addition, the MasPar MP-1 has hardware support for PEs to make indirect memory references, and this makes the CSI technique much more effective.

Throughout the rest of this paper, we use CSI to refer to CSI for a SIMD target machine.

3. The CSI Algorithm

The CSI algorithm analyzes a segment of code containing operations executed by any of multiple threads (enabled sets of SIMD PEs). From this analysis, it determines where threads can share the same code and what cost is associated with inducing that sharing. Finally, it generates a code schedule that uses this sharing, where appropriate, to achieve the minimum execution time. Unfortunately, this implies that the CSI algorithm is not simple.

Our prototype CSI tool implementation is also quite complex. It implements **only** CSI on assembly-level tuples —it is not a compiler and does not even perform fi nal register allocation. Written in C using PCCTS [15], the prototype consists of over 8,000 lines of C source code.

3.1. Example Code Segment

In order to make the CSI algorithm more clear, the description of each major step in the algorithm is accompanied by a simple example code segment processed up to that stage in the CSI algorithm. The example code is not particularly meaningful, but clearly demonstrates the algorithm. The code is:

this high-level C-like parallel code corresponds to assembly-level code like:

"then" clause			else clause		
c = a + b;			c = a - b;		
0	const	#a	0	const	#a
1	load	0	1	load	0
2	const	#b	2	const	#b
3	load	2	3	load	2
4	add	1,3	4	neg	3
5	const	#c	5	add	1,4
6	store	5,4	6	const	#c
			7	store	6,5

In executing this code, first the value of *parallel_expression* would be computed on all currently enabled processing elements (PEs). Next, the set of enabled processors would be masked down to only those for which *parallel_expression* evaluates as true. Only these PEs would execute c = a + bi. Having completed the "then" clause, the SIMD machine would prepare to execute the else clause by changing the enable mask so that only PEs whose *parallel_expression* is false are enabled. After these PEs have executed c = a - bi, the enable mask is restored to its state prior to entering the if. Hence, the time taken within the if statement clauses is essentially the time for the "then" clause + the time for changing the enable mask + the time for the else clause.

In contrast, the CSI optimization attempts to bring the execution time as close as possible to *maximum("then"* time, else time), which would be the time taken if both clauses could be executed simultaneously without masking overhead.

Since the CSI optimization is explicitly based on minimizing execution time, we also need to associate a cost with each operation. In this paper, we use the approximate execution times of the instructions counted in units of machine cycles for a MasPar MP-1 [3]. Note, however, that our instructions do not match those of the MasPar and we do not model the overlap that the MasPar allows between memory references and other PE operations. Hence, these times are realistic, but only approximately correspond to MasPar times. Given that disclaimer, the execution time for the above code is:

Then time		615
Mask time	+	9
Else time	+	639
		1263 clock ticks

and our goal is to use CSI to reduce the time to be as close as possible to *maximum*(615, 639), or 639 clock ticks. If this goal is achieved, the execution time of the code would be reduced by a factor of 49%.

3.2. Algorithm Walk-Through

Sections 3.2.1-3.2.8 detail each major step in the CSI algorithm as it is currently implemented in our prototype CSI tool. The state of the above example is given with each step's description.

The algorithm can be summarized as follows. First, a guarded DAG is constructed for the input, then this DAG is improved using inter-thread CSE. The improved DAG is then used to compute information for pruning the search: earliest and latest, operation classes, and theoretical lower bound on execution time. Next, this information is used to create a linear schedule (SIMD execution sequence), which is improved using a cheap approximate search and then used as the initial schedule for the permutation-in-range search that is the core of the CSI optimization.

3.2.1. Step 1: Construct Guarded DAG

The first step in the CSI algorithm is the construction of a guarded DAG for the assembly-level operations. The use of a DAG, Directed Acyclic Graph, to represent data dependencies has long been a standard technology for optimizing compilers [1]; however, the concept of a guarded DAG is somewhat unusual. Normally, each node in a DAG represents an operation and each arc represents data fbwing between operations. It is assumed that *every operation is executed if any operation is executed*. This is not true for the code of a traditional *if* statement.

However, in the SIMD view, every operation within a parallel if is executed if any operation is $executed^{(b)}$. The catch is that operations may be executed by different sets of PEs. Hence, we need some way of tracking which PEs will execute which instructions.

We do this by associating a unique guard value with the alternative path selected by each conditional expression in the code segment. These guard values are then encoded as individual bits. It is then possible to tag each instruction with a guard which is the "or" of the guard values that dominate its execution. In this way, code with arbitrary forward branching can be analyzed as a single DAG in which each node is tagged with its guard value. For example, consider the guard markings in listing 1.

```
/* guard 1 2 4 8 16 */
if (parallel_expression1) {
    /* guard 1|2|4|8 */
    switch (parallel_expression2) {
             /* guard 1 */
    case A:
                                break;
    case B:
              /* guard 2 */
    case C:
             /* quard 2|4 */
                                break;
    default: /* guard 8 */
                                break;
    }
    /*
       guard 1 2 4 8 */
} else
       {
       guard 16 */
    /*
/* guard 1|2|4|8|16 */
```

Listing 1: Example of Guard Labeling

Neither multi-way branches (parallel cases) nor nested conditionals is a problem. Loops, which are formed by backward branches, require that the inside of the loop be handled as a separate problem from the code before and after the loop. A similar difficulty occurs when independent conditional statements are executed in a sequence, rather than nested; in such a case, the easiest solution is to analyze the conditionals separately^(c). Although the examples in this paper have no more than two threads (guard bits), the current prototype CSI tool can process arbitrary guarded input with up to 32 threads.

Returning to our example if statement, the result is the guarded DAG of figure 1.

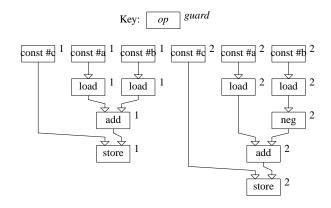


Figure 1: Original Guarded DAG for Example

⁽b) Some SIMD languages implicitly perform a test to see if any PE will be enabled and jump over the clause if none will be enabled. For example, this is the definition used by MPL for parallel if statements [10]. Here, we assume that no such test and jump is made.

⁽c) It is actually better to modify the guard handling so that this case can be analyzed intact, but that is much more complex, and has been omitted from the algorithm in this paper.

3.2.2. Step 2: Inter-thread CSE

Given a guarded DAG, the next step is very similar to recognizing and factoring-out 'common subexpressions." However, it is not quite traditional CSE, because **operations with different guards can be factored-out as common subexpressions**. Hence, we call this step 'inter-thread CSE," although the effect is more like a combination of conventional CSE and code hoisting (except we don't need a dominator or code motions).

Whereas traditional CSE recognizes when two computations would produce the same value, inter-thread CSE recognizes when two computations would produce the same value *if* they were executed by the same processor. For each interthread common subexpression, the remaining operation is given the guard that is the 'or' of the guards for all operations absorbed by that optimization.

This works because, even though operations with different guards may be executed on different PEs, the instruction sequence that combines one PE's local data in a particular way must perform the same function for another PE working on its local data. If the guards have bits in common, it simply means that traditional CSE was performed on some PEs.

After inter-thread CSE, the cost of the example drops from 1263 to 891 clocks^(d); a 29% reduction. The resulting guarded DAG is given in fi gure 2.

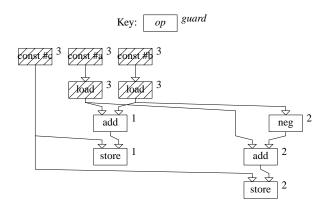


Figure 2: Guarded DAG After Inter-Thread CSE

3.2.3. Step 3: Earliest and Latest Computation

After performing inter-thread CSE, there are a few search pruning characteristics that need to computed before the CSI search phase is begun. Perhaps the most basic of these are earliest and latest.

The CSI search operates on a linear schedule of the instructions, rearranging that linear schedule and considering combining only those instructions which are adjacent in the linear schedule. This implies a permutation search. The problem is simply that even a small CSI example, such as the one used in this paper, would yield too large a search space if a complete permutation search was used. Using a full permutation search on the small example in this paper would require consideration of 10!, or 3,628,800, linear schedules; the larger example given in section 4 contains 23 instructions, hence, 23! (25,852,016,738,884,976,640,000) different schedules would need to be examined. Without very effective pruning, CSI is infeasible.

One of the most effective pruning methods is to simply eliminate the linear schedules that violate the precedences expressed by the DAG —for example, any linear schedule that places the neg operation before const #b is invalid and need not be considered. The problem is that to check each schedule for validity using the DAG is relatively expensive because we would still have to generate the bad schedules in order to check them. The earliest and latest measures provide a way of performing a somewhat conservative version of the DAG check without actually generating the schedules that would fail the test.

Earliest for an operation is the earliest position in the linear schedule which that operation could occupy without violating the DAG, in other words, it is the number of DAG predecessors. Latest is the latest viable position for that operation in the linear schedule, which is equivalent to the total number of operations minus the number of operations which have that operation as a predecessor (including the operation itself). Rather than performing an ordinary permutation search on the linear schedule, a permutation-in-range can be used, restricting each operation to move only through slots in its earliest to latest range.

For our example, the result of earliest and latest labeling is shown in figure 3.

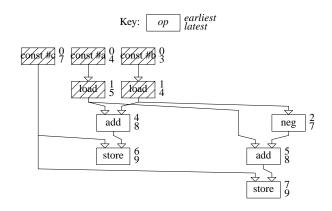


Figure 3: Earliest and Latest Labeling of the DAG

We applied a similar technique to reduce the search space for generation of optimal code schedules for pipelined machines. An overview of this code scheduling technique applied to pipelined machines appears in [13]; a more detailed treatment, including a proof that optimal schedules are obtained, is given in [14].

⁽d) Actually, 891 is the cost obtained after conversion to a linear schedule in step 6 (section 3.2.6), but this number reflects only the benefit gained by the use of inter-thread CSE.

3.2.4. Step 4: Classification

Just as the earliest and latest information is used to prune a search, it can save a significant amount of time if operations are grouped into classes prior to the start of the search. Each class consists of a set of operations such that it is allowable for each operation in that class to be merged with at least one other member of that class. Hence, if two operations are not in the same class, there is no need for a more detailed (and more expensive) check to determine if they could be merged.

Classes are formed to be as small as possible so that for each class:

- 1. The opcodes for all members of this class are the same.
- 2. The immediate operands, if any, for all members of this class are the same.
- 3. The class members cannot be partitioned such that the operations in some partition element all must execute after all the operations in some other partition element. Using the DAG, this is quite complex to check; hence, we use a conservative approximation.

If the members of a class are sorted by earliest as the primary key and latest as the secondary key, one can simply check that each pair of adjacent operations in the class have overlapping earliest..latest ranges. If the ranges do not overlap, then the class can be partitioned into two classes by splitting it between the nonoverlapping adjacent operations.

Every operation whose guard covers all other guards within its class can be made into a singleton class.

As a simple approximation to this, we used the rule that an operation whose guard is all threads is a singleton class.

5. All members of this class do not have a thread in common. If they do, each should be its own singleton class.

The first two conditions are a direct consequence of basic SIMD execution: the same information must be broadcast to all PEs. Condition 3 reduces classes by applying DAG constraints. The 4th and 5th conditions actually follow from the observation that after CSE, no two instructions that can be executed by the same thread can be merged; if they could be, they would have been factored-out when inter-thread CSE was performed.

The class formation procedure simply applies rules 1 and 2 to create initial class groupings and then recursively attempts to reduce these classes using rules 3, 4, and 5. The result for our example code is shown in figure 4.

3.2.5. Step 5: Theoretical Lower Bound

Using the classes and expected execution times for each type of operation, it is possible to compute a good estimate of the lower bound on minimum execution time. This estimate can be used to determine if performing the CSI search is worthwhile —i.e., if the potential for improvement in code execution time by CSI is small, then one might abort the search. The same algorithm is used to evaluate partial schedules to aid in pruning the search.

The estimate is computed by:

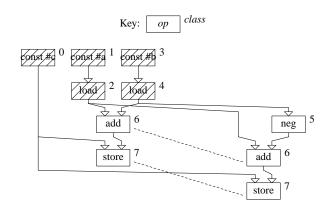


Figure 4: Classifi cation of Operations in the DAG

- 1. For each class, group members together if the guards do not overlap.
- 2. The cost for each class is the number of members remaining times the cost of that operation.

This bound might be unachievable because it ignores detailed dependence constraints (DAG checks) and it ignores the cost of masking, but it is quick to compute and the estimates are usually very close to the best achievable execution time.

The minimum number of instructions remaining after CSE, or minimum 'ticks', is also computed at this stage.

For the simple example if statement, the computed lower bound is 639 clock ticks, resulting in a total of 8 instructions after CSI.

3.2.6. Step 6: Creation of An Initial Schedule

Before the search can be performed, the code must be converted into a linear schedule. In the linear schedule, the N^{th} operation in a schedule is either executed at the same time as the $(N-1)^{\text{th}}$ instruction or in the next "tick." There are two reasons that a linear schedule is used:

- 1. The permutation-in-range search (step 8, section 3.2.8) is relatively efficient using the linear schedule.
- 2. The linear schedule corresponds to a SIMD execution sequence, and this instruction sequence must be examined in order to compute an accurate cost. There is a great temptation to view CSI as a graph node matching problem on the DAG, but combining some graph nodes implies a significant cost which is not computable without the linear order.

When two nodes (operations) are combined, it might not be possible for the operands to be directly placed in the same registers under both original guards. Hence, it may be necessary to insert one or more register-to-register moves that would be executed under one of the guards. This may, in turn, involve additional cost for masking —unless the register-to-register move can be executed immediately before or after another instruction that has the same guard. Since these costs depend on properties of the SIMD (linear) schedule, and these costs can easily outweigh the benefit of combining, the linear schedule must be examined. Hence, in this step we convert the DAG into a linear schedule.

The linear schedule is created by performing a level-order traversal of the DAG, but in this traversal operations in the same class as the previous operation in the schedule are given preference. This tends to group together instructions that could be combined by CSI.

3.2.7. Step 7: Improving the Initial Linear Schedule

Although any linear schedule that does not violate the DAG constraints would be valid as input to the search, cost pruning is used and finding a better schedule earlier will cause more pruning. This makes it worthwhile to invest a little effort in making the initial schedule relatively good.

Currently, the prototype CSI tool performs a 'sort" of the schedule generated in step 6. Instead of using comparison of key values, in this 'sort," elements in the schedule exchange places only if the exchange reduces a very crude estimated cost. This portion of the CSI tool is a 'hack," but it does tend to significantly improve the schedule, and hence improves pruning in the 'real" search.

At this stage, the code for the simple if example has been restructured so that it requires only 690 ticks. This represents an additional reduction of 23% over the improvement due to inter-thread CSE, or a total improvement of 45% as compared to the original code.

3.2.8. Step 8: The Search

Given the information determined in the previous steps, we are now ready to perform the permutation-in-range search for the minimum execution time schedule. The technique presented here is very similar to that which we used in code scheduling for pipelined machines [13][14], except in that the pruning and cost criteria are different and we have the extra dimension of considering merges of adjacent instructions.

For the search, the initial *N*-operation linear schedule is partitioned into two parts: the *n*-operation partial schedule under evaluation (schedule slots 0..n-1) and the portion of the schedule that has not yet been evaluated (*n*..*N*-1). The basic step in the permutation-in-range search is to consider swapping the instruction in slot *n* with any of the instructions in slots greater than *n*. Whenever a viable swap is found, the incremental change to the partial schedule is evaluated. A viable swap causes the partial schedule to be extended by moving the partition to between slots *n* and *n*+1; a swap that cannot lead to a better complete schedule prunes all schedules with that *n*-operation prefix.

The main components of the search are:

- Only consider swaps for which the instruction being swapped into the partial schedule at position *n*-1 has earliest≤*n*-1 and the instruction being swapped out has latest≥*n*. Note that if this condition is not met, then not only is the swap disallowed, but additional pruning is possible.
- 2. Only swaps that do not violate the DAG precedences are valid.

- 3. As each operation is added to the partial schedule, it might either execute in the tick after the previous operation. Alternatively, if it can merge with that operation, it would execute in the same tick. Merges are permitted only if the operations are in the same class and there are no DAG or guard conflicts (i.e., no instruction being merged is the predecessor of any other instruction being merged and none of the guards overlap).
- 4. In a machine (like the MasPar) in which combining usually is beneficial, give precedence to swapping-in operations that are of the same class as the previous operation.
- 5. For much the same reason given in rule 4, when a merge of instructions into the same tick is possible, the merger is evaluated before the non-merged schedule.
- 6. Because merging happens with adjacent operations in the linear schedule, if there are k instructions that can merge into one, there are k! different possible orderings in which they might appear with the same result. This would multiply the search time by k!. Hence, merges are only allowed if the operations being merged are in order of increasing internal identifier. For example, merging tuples 4 and 12 (the add operations in the example) will be allowed only if their order in the linear schedule is (4, 12), not if their order is (12, 4).

This reduces the search space equivalently to using ticks, rather than schedule slots, for the linear schedule. However, since the number of slots is fixed and the number of ticks varies, the slot scheme with this adjustment yields a more efficient search.

7. A swap that must result in a schedule worse than or equal to the best found thus far need not be investigated further. Hence, if the cost of the current partial schedule + the theoretical minimum cost of the operations remaining to be scheduled \geq cost of the best complete schedule found thus far, the swap is considered invalid.

Note that computing the cost involves more than just observing whether a merge is possible; it is also necessary to compute the approximate overhead in placing operands in the same registers for the merged operations. The masking and register move cost computation used in this paper is simply that each operand that cannot be trivially renamed to be in the appropriate register adds the cost of one registerto-register move + one mask operation unless the previous instruction has the same guard. This is a gross oversimplification of how it should really work (see section 3.4), but the ideal register allocation process is too complex to describe in this paper and the method described here produces acceptable results.

All of these techniques have the property that they will never prune a unique optimal schedule. Hence, if allowed to run to completion, the technique is equivalent to an exhaustive search and ensures that the optimal schedule will be found.

Despite the pruning, running to completion is not always feasible. We suggest that in such cases an upper limit should be placed on the number of operation swaps considered. That limit could be a fixed number or, perhaps more useful in practice, it could be derived based on the level of optimization specified by the programmer and the amount of potential improvement estimated by the theoretical bound.

3.3. Final Output for Simple Example

After the search has completed (or been artificially terminated before completion), the resulting linear schedule is the SIMD program. In the version of the CSI prototype described here, the SIMD program need only have registers assigned and masking and register move code inserted.

The linear schedule output by the CSI prototype tool for the simple if example is:

```
;Initial cost = 1263
;Cost after inter-thread CSE = 891
;Theoretical lower bound ticks = 8
;Theoretical lower bound cost = 639
;At perm #11, new cheapest is 690...
;At perm #21, new cheapest is 666...
;Final Tuples (651 perm calls, cost 666):
code
                          ;tick 0
3:0
        const
                 #a
3:2
        const
                 #b
                          ;tick 1
3:5
                 #c
                          ;tick 2
        const
3:1
                 0
                          ;tick 3
        load
3:3
        load
                 2
                          ;tick 4
2:11
                 3
                          ;tick 5
        neq
1:4
        add
                 1,3
                          ;tick 6
2:12
        add
                 1,11
                          ;tick 6
                          ;tick 7
1:6
                 5.4
        store
2:14
        store
                 5,12
                          ;tick 7
```

The format is *guard*: *operation* ; *tick*. Notice that the search ran to completion in just 651 swaps (1 swap \equiv 1 perm call) and only the Neg instruction is not executed by all PEs. The result is 47% faster than the original code.

However, there is also an unpleasant little surprise: the ideal execution time was not achieved. The execution time is 666 clocks when it should have been 639. The reason has to do with a nasty complication concerning register allocation and the concept of "register liveness."

3.4. Partial Liveness

In a conventional machine, a register either holds a live value or it is free for reuse. In a SIMD machine (or any parallel machine), a register can be live or dead for any guard, and can be simultaneously live with different values in different threads. We call this new concept "partial liveness" and it is responsible for the difference between 666 and 639 clocks for our simple example.

To better understand this, consider the DAG showing the fi nal state of the example (see fi gure 5). Notice that the register holding the result of loading b is used in two places: by Neg and by Add. In the linear schedule (see above), the Neg instruction comes *before* the Add. Hence, when allocating a register for the result of the Neg instruction, conventional liveness analysis fi nds that the register holding the loaded value of b is still live and that register cannot be reused for the result of the Neg. Hence, the result of Neg is placed in a different register and then copied back for the Add. In order to merge Add operations 4 and 12, a register-toregister move is inserted to move the result of Neg into the same register that holds the loaded value of b on the other thread. 666 is simply 639 + the move overhead.

Had our CSI tool been smarter, it would have realized that the register holding the loaded value of b is only partially live after the Neg instruction, hence, it could have been reused without conflict. That knowledge would have allowed it to achieve the 639 clock theoretically optimal time; an execution time reduction of 49%.

Unfortunately, partial liveness in the context of CSI becomes much more complex as larger codes are considered, hence, it will have to be the topic of a future paper. In this paper, we assume the traditional definition of liveness — and suffer the penalty.

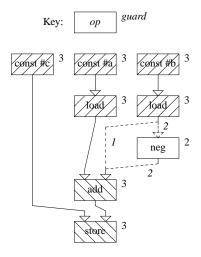


Figure 5: DAG Showing Final State of Example

4. A Bigger, Tougher, Example

While the example case used to illustrate the CSI algorithm obtained a good speedup, it is not clear how often the code sequences for different threads will look that similar. Neither is it clear that any performance is gained when the threads differ more significantly.

We do not have statistics available on how often threads have very similar code, although it seems fairly likely that SIMD code involving tests for 'edge conditions' would have this property. To answer the question of how performance degrades with larger, less symmetrical, code, we present listing 2. Here, only the lvalue of a and the rvalue of c are inter-thread CSEs. The 'then' clause even has one more memory reference than the else clause.

The interesting result is that CSI works nearly as well as it did on the simple example. This is primarily because the MasPar supports indirect memory references, so all memory references can be merged. Such merges are usually profitable because the PE local memory interfaces on the MasPar MP-1 are shared by groups of PEs [3], often making memory

"then" clause			else clause			
a = *b + c; d = a + d;			a = e =	c + e; f - g;		
0	const	#b	0	const	#c	
1	load	0	1	load	0	
2	load	1	2	const	#e	
3	const	#c	3	load	2	
4	load	3	4	add	1,3	
5	add	2,4	5	const	#a	
6	const	#a	6	store	5,4	
7	store	6,5	7	const	#f	
8	const	#d	8	load	7	
9	load	8	9	const	#g	
10	add	5,9	10	load	9	
11	store	8,10	11	neg	10	
			12	add	8,11	
			13	store	2,12	

Listing 2: A More Diffi cult Example

reference time the performance-limiting factor. In addition, performance is helped by the fact that enable masking and registerto-register moves are both quick operations.

The initial code would have taken 2478 clocks. Interthread CSE by itself would only have reduced that by 7%, to 2312; after the sort described in step 7 (section 3.2.7), the reduction would have been just 13%, to 2159. However, the full CSI algorithm gives an impressive performance, reducing the time to just 1386 clocks —a 44% reduction.

Unlike the simple example, in this case the search did not run to completion, so optimality is not guaranteed. The algorithm examines swaps at a rate of about 20μ s/swap running on a SPARC server, and was allowed to run for 1,000,000 swaps (20 seconds). A total of just 21 complete schedules were considered —this should be contrasted with the 23! possible schedules. In fact, the search very quickly yields good answers; over half the improvement (a schedule requiring just 1803 clocks) was achieved after performing only 106 swaps and examining just fi ve complete schedules. For this reason, the prototype CSI tool is even effective in helping to optimize SIMD programs that have over a hundred instructions and many threads [6].

4.1. Recursive CSI

While good performance was obtained using the CSI algorithm in this paper, still better pruning would be desirable. One obvious approach is to partition the original CSI problem into two or more parts, schedule each independently from the others, and then apply the CSI algorithm to the concatenation of the schedules for each part.

The CSI prototype implementation does not automatically provide this recursive subdivision, but can read its output as input. Hence, we were able to perform a simple experiment by hand-partitioning the original code into two parts, using CSI on each, and then using CSI on the catenation of the two outputs. Although essentially the same final schedule was obtained, the recursive application did cause a faster pruning, and the number of swaps totaled for all three CSI runs was less than that for the single CSI run over the complete initial code.

The problem is that the improvement in search speed by recursive subdivision is critically dependent on choice of partitioning, and we do not yet have a good method by which the partitions can be mechanically generated.

4.2. Simulated Annealing

Another possible way to speed convergence of the search is to modify the driver from section 3.2.8 to use a simulated annealing approach. Notice that all the pruning methods can still be applied, but the benefit would be somewhat less than in the current search. All pruning in the simulated annealing would be pruning complete schedules, whereas permutation-inrange can incrementally prune a partial schedule and all complete schedules that contain it. We have not yet implemented a simulated annealing prototype.

5. CSI To Increase Vector Length

Thus far, this paper has discussed CSI as a method to improve the execution speed of SIMD conditionals. In this section, we suggest that the same technology, combined with careful data layout, is also the key to creating long vector operations out of short vector operations, or even vector operations out of scalar references.

Suppose one has a 16,384-PE machine and SIMD code:

```
int al[8192], a2[8192];
int bl[8192], b2[8192];
int cl[8192], c2[8192];
c1 = a1 + b1;
c2 = a2 - b2;
```

To get the best memory utilization, this should result in a memory layout like that shown in figure 6.

PE0	PE1	PE2	PE8191	PE8192	PE16383
a1[0]	a1[1]	a1[2]	a1[8191]	a2[0]	a2[8191]
b1[0]	b1[1]	b1[2]	 b1[8191]	b2[0]	 b2[8191]
c1[0]	c1[1]	c1[2]	c1[8191]	c2[0]	c2[8191]

Figure 6: Memory Layout for 8,192-Element Arrays

However, given 16,384 PEs, it makes sense to imagine that each memory object is 16,384 elements in width. This renaming of the memory cells gives the layout depicted in figure 7. This is interesting because reflecting this renaming back into the source program yields:

PE0	PE1	PE2	PE8191	PE8192	PE16383
a[0]	a[1]	a[2]	a[8191]	a[8192]	a[16383]
b[0]	b[1]	b[2]	 b[8191]	b[8192]	b[16383]
c[0]	c[1]	c[2]	c[8191]	c[8192]	c[16383]

Figure 7: Memory Layout for 8,192-Element Arrays

```
int a[8192 + 8192];
int b[8192 + 8192];
int c[8192 + 8192];
if (PE_number < 8192) {
    c = a + b;
} else {
    c = a - b;
}
```

which is exactly the same if statement that was used for the simple example in section 3.1 of this paper.

Admittedly, there is much work to be done before CSI can be combined with sophisticated data layout to mechanically lengthen vectors, but this gives a clear direction for future research.

6. Summary and Conclusions

CSI was originally proposed in [7], but no practical algorithm had been found until April 1991. The algorithm is not simple, and certainly can be improved further, but our prototype implementation has shown CSI to be both feasible and surprisingly effective in at least a few test cases.

In some sense, CSI is the most fundamental compiler transformation for a SIMD, because it merges threads to keep PEs enabled. It does this by merging instructions from different paths within then and else clauses, multiway branches, and even nested conditionals. Coupled with new techniques for data layout, it should also be possible to use CSI to create "vectors" out of groups of ordinary scalars, and longer vectors out of multiple short vectors.

In addition, the CSI prototype implementation has exposed an important defect in current compiler technology for parallel machines: the inappropriateness of using ordinary liveness for register allocation. As a solution, we have introduced the concept of 'partial liveness'' to more accurately manage register usage, especially in SIMD machines.

Finally, it is useful to recall that variations on CSI apply to a fairly wide range of architectures (see section 2), not just SIMD. Perhaps the generality of CSI will lead to research on other new compiler transformations based on analysis of code (operations), rather than the far more common analysis of values (data fbw analysis) or of storage locations (dependence analysis)?

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